

Roll No.

97667

B.C.A. 2nd Semester

Examination-May, 2017

**Mathematical Foundation of Computer
Science**

Paper-BCA-108

Time : 3 hours

Max. Marks : 80

Before answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard will be entertained after the examination.

Note : Attempt **five** questions in all. Question No. 1 is **compulsory** and attempt **four** more questions by selecting **one** question from each unit. All questions carry equal marks.

1. Compulsory question

(a) What do you mean by Correlation ? List various types of correlation.

(b) Find the median for the series:
10, 12, 8, 9, 70, 60, 40, 80.

(c) What is a Graph ? Explain with the help of an example.

(d) What is Weighted Graph ?

(e) What is a Tree ? What are its properties ?

(f) What is Merge Sort ?

(g) What is LHRRWCC ?

(h) Find the first four terms of a sequence from the Recursive Formula:

$$a_n = 5a_{n-1}, \quad n \geq 1 \quad \text{with the initial condition } a_0 = 8$$

UNIT-I

2. (a) In a study on patients, the following data were obtained. Calculate the arithmetic mean.

Age in Years	10-19	20-29	30-39	40-49	50-59	60-69	70-79	80-89
No. of Cases	1	0	1	10	17	38	9	3

(b) Find the median of the following frequency distribution.

Marks	0-10	10-20	20-30	30-40	40-50	50-60
No. of Students	15	17	19	27	21	15

3. (a) The Mean and Variance of 7 observations are 8 and 16 respectively. If five of the observations are 2, 4, 10, 12, 14, find the remaining two observations.

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(3)

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- (b) Calculate Karl Pearson's coefficient of correlation for the following data:

x:	5	10	15	20	22	25	30
y:	10	12	8	7	6	5	3

UNIT-II

4. (a) Describe the method for analyzing an algorithm. What do you mean by best case and worst case time complexity of an algorithm ?
- (b) Define linear search algorithm. Find the number of comparisons required to search 9 in the sequence 1, 3, 4, 5, 6, 8, 9, 11 using linear search.

5. (a) Prove that the degree of any vertex in a simple graph of 'n' vertices cannot exceed $n-1$.
- (b) Define Isomorphic and Homeomorphic graph with the help of a example.

UNIT-III

6. (a) What is Spanning Tree? Explain the various methods for constructing spanning tree for a connected simple graph.
- (b) Draw a binary tree for the following Preorder and Inorder traversals:
Preorder: D E B F C A
Inorder: D B E A F C.
7. (a) (i) Convert the decimal number $(76.25)_{10}$ into binary number.

(110101)₂ into decimal number.

- (b) Explain the algorithm for bubble sort and use bubble sort to put the elements of the list 7, 8, 4, 6, 1, 0, 9 in increasing order.

UNIT-IV

8. (a) Solve the recurrence relation:

$$a_n + 2a_{n-1} + a_{n-2} = 0, \text{ for } n \geq 2.$$

- (b) Using Principle of Mathematical Induction, prove that:

$$1.2.3 + 2.3.4 + 3.4.5 + \dots + n(n+1)(n+2)$$

$$= \frac{n(n+1)(n+2)(n+3)}{4}, \text{ for all } n \in \mathbb{N}.$$

9. (a)

as a linear combination of numbers.

- (b) Solve the congruence: $13x \equiv 10 \pmod{29}$